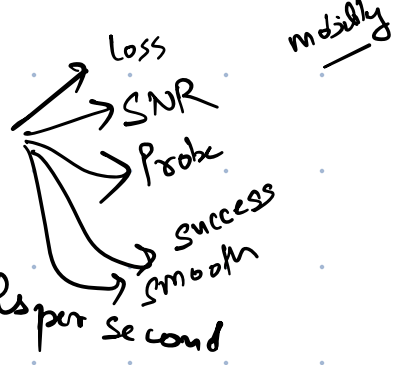


CS 598 WSI, Lecture 4

- Rate adaptation
- Frequency and bandwidth
- Narrowband vs. wideband
- OFDM: Motivation.

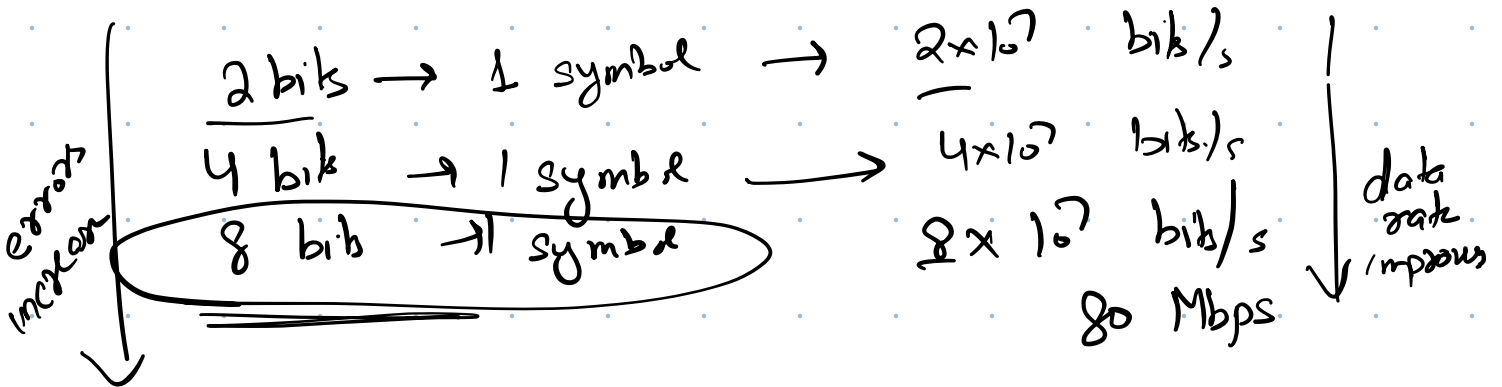
Rate Adaptation



Symbol rate: $\rightarrow 10\text{MHz} \rightarrow 10^7$ Symbols per second
 \hookrightarrow hardware/protocol

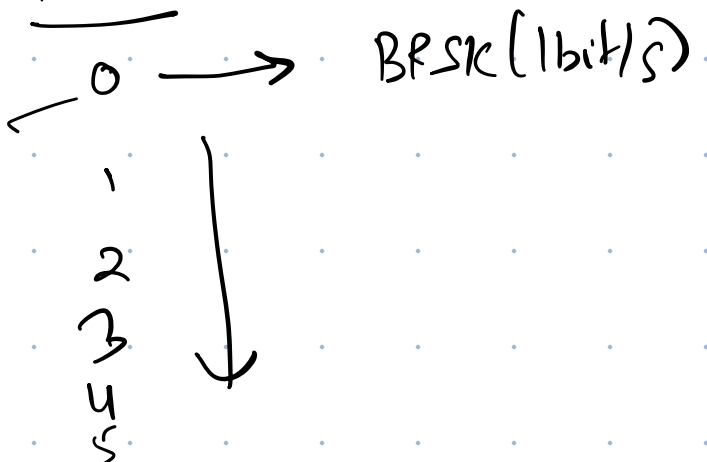
Modulation

bits \rightarrow symbols (complex-valued)



really low data rate \rightarrow losing throughput
 " high " \rightarrow lose throughput
 modulation and coding.

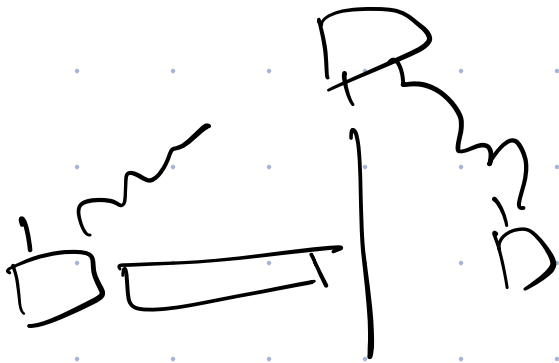
MCS (Modulation and coding scheme)
 $1/2 \rightarrow$ data rate



2
Q. How do you know your data rate is too high?
losses / no acks.

Q. ... too low?
too much success, try something better

Losses \implies reduce data rate | SNR-based
increase or reduction.



(Probing to increase data rate)

False

Sample Rate

MCS	Success rate	Table
6	→ 99.5%	$99.5\% \times 10\text{Mbps}$ $= 9.95\text{Mbps}$
7	→ 95% 99%	
8	→ 90%	
9	→ 85%	$8.5\% \times 40\text{Mbps}$ $= 34\text{Mbps}$

vs

Sample rate

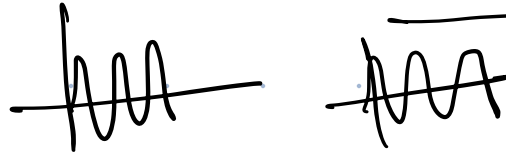
Naive
 7 n n n
 8 n

8 n n n
 9 n n n n

Sample rate
 7 n n n n
 x 10

Frequency vs Bandwidth

Wi-Fi operates at $\frac{2.4\text{GHz}}{5\text{GHz}}$



bandwidth \rightarrow how many samples/symbols can I send per second.

$20\text{MHz} \rightarrow 20 \times 10^6$ symbols/s

$40\text{MHz} \rightarrow 40 \times 10^6$ symbols/s

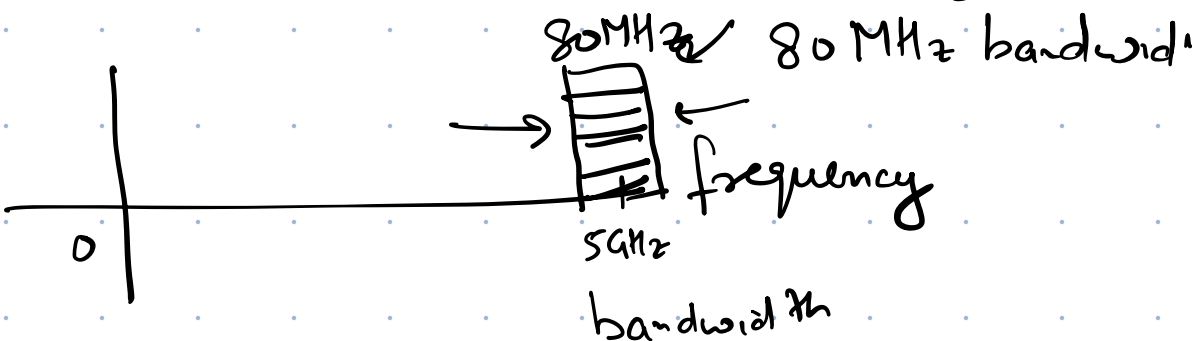
$80\text{MHz} \rightarrow 80 \times 10^6$ symbols/s

(160/320)

80 MHz bandwidth at $\approx 5\text{GHz}$.

$5\text{GHz} - 40\text{MHz}$, $5\text{GHz} + 40\text{MHz}$

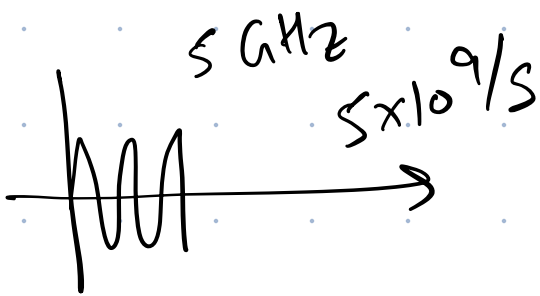
\hookrightarrow occupied by this signal.



Q. Why choose 20MHz or 80MHz?

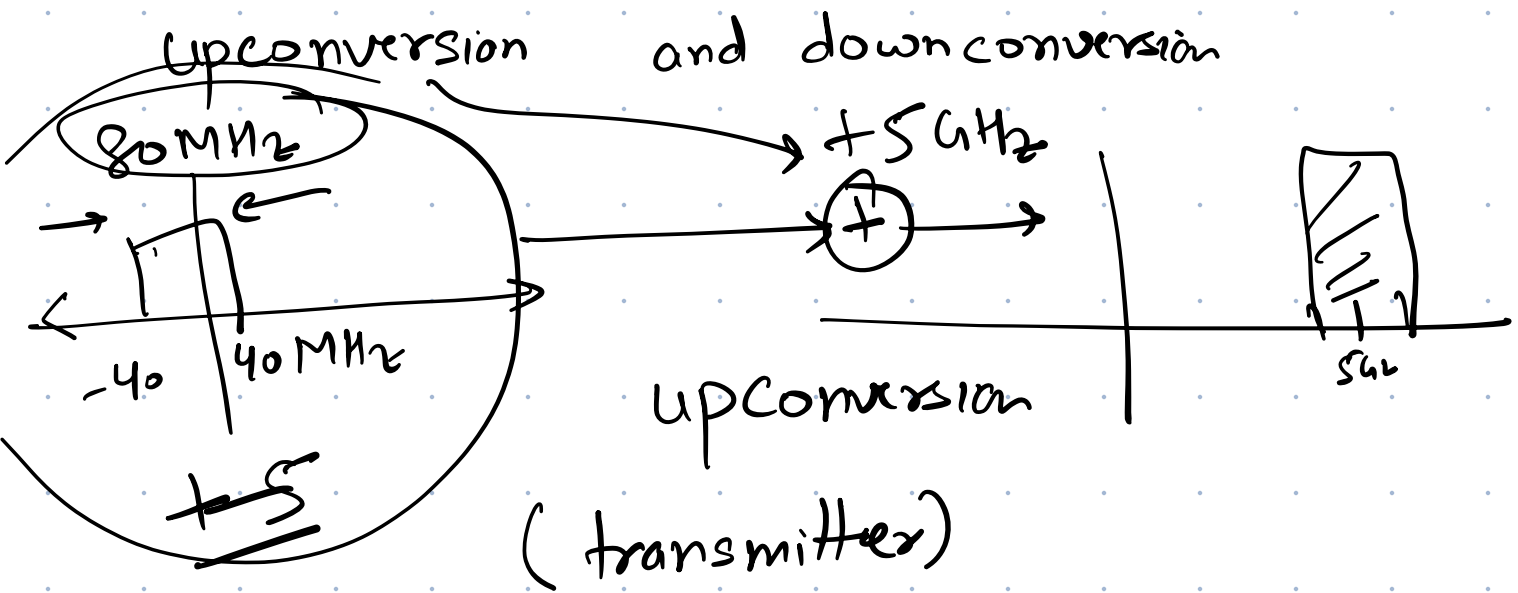


$20 \times 10^6 \text{ symbols/s} \rightarrow 80 \times 10^6 \text{ symbols/s}$
4 times more data

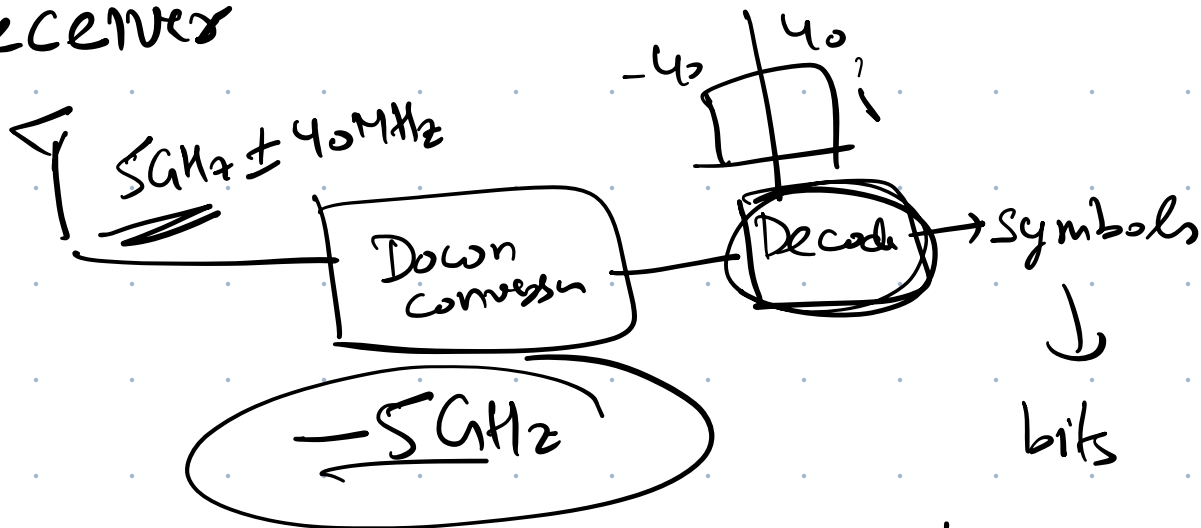


hardware that samples my signal at $5 \times 10^9/s$.

- power-hungry.
- expensive



Receiver



Transmit and receive directly at

80MHz?

Spectrum?

Channels 5GHz, ~~5GHz~~ 5GHz + 80MHz

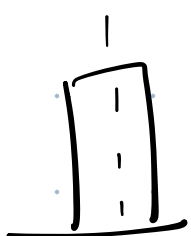
5GHz + 40Hz

5GHz + 120

Antenna \sim wavelength

$$80\text{MHz} = \frac{3 \times 10^8}{80 \times 10^6} = \frac{300}{80} \approx 4\text{m.}$$

$$5\text{GHz} = 6\text{cm}$$



 $B' \approx 80 \text{ MHz}$

 $f_c \approx 5 \text{ GHz}$

 got $0.001 \text{ MHz} = 1 \text{ kHz} = 10^3 \text{ Hz}$

 $\approx 5 \text{ GHz} + 1 \text{ kHz}$

 $f_c - \frac{B}{2}$ to $f_c + \frac{B}{2}$

Receiver = $(-f_c)$ $-\frac{B}{2}$ to $\frac{B}{2}$

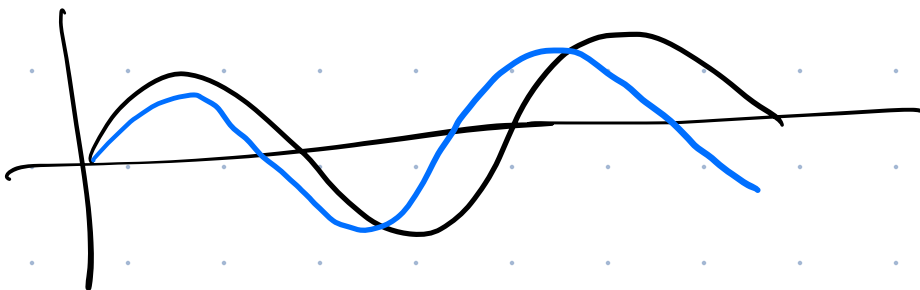
 $5 \text{ GHz} - 1 \text{ kHz}$

$f_c - f_c' =$ Carrier frequency offset (CFO)

 Carrier frequency

$B \approx$ sampling frequency

 B sampling frequency offset (SFO)



Recap: Wireless Channel

$x_1, x_2, x_3, x_4, \dots, x_N$

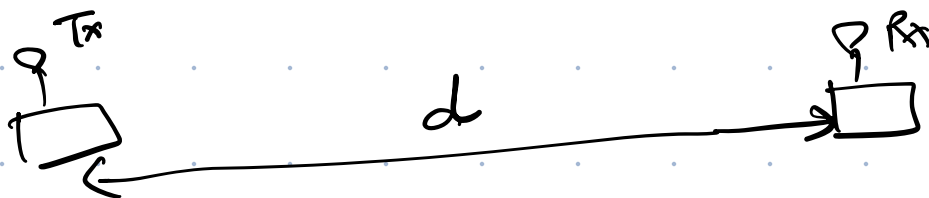
y_1, y_2, \dots, y_N

$$y_i = h x_i + n_i$$

↳ wireless channel

(impact of the environment)

↳ What does h tell us about the environment?

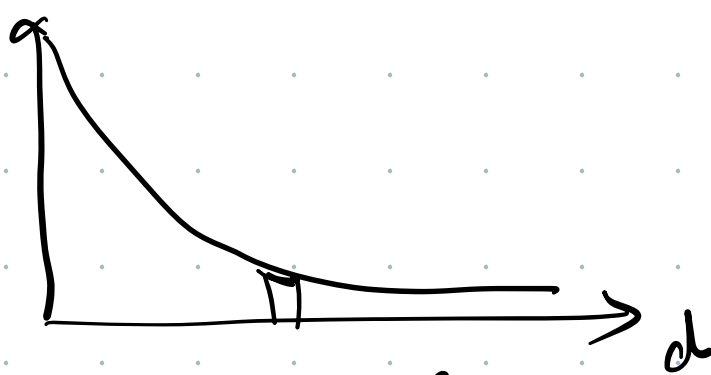


h is a complex number.

amplitude = strong or weak?

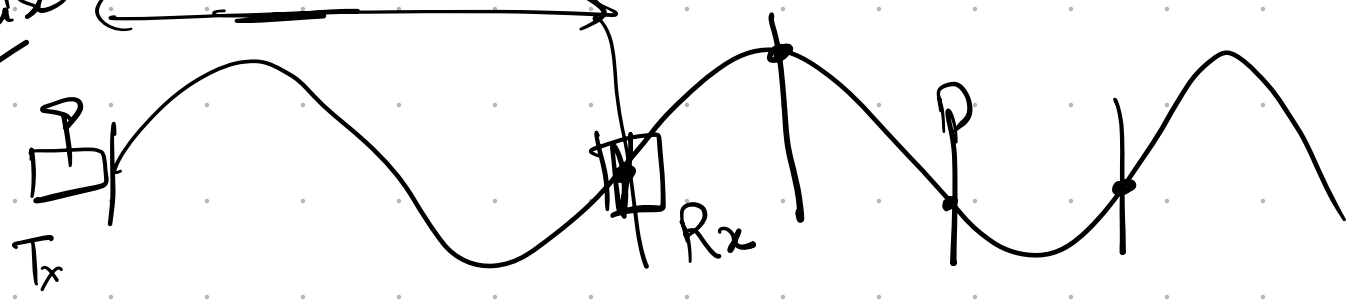
$$\rightarrow |h| \propto \frac{1}{d}$$

$|h|$

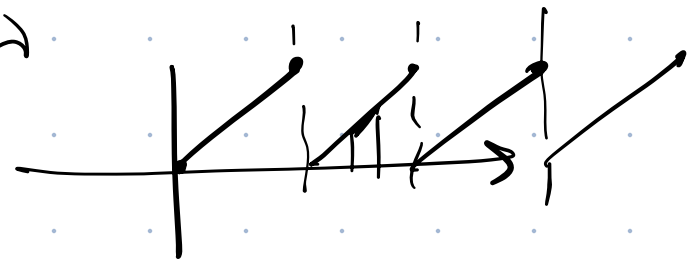


$\lambda = 8 \text{ cm} \text{ (5 GHz)}$

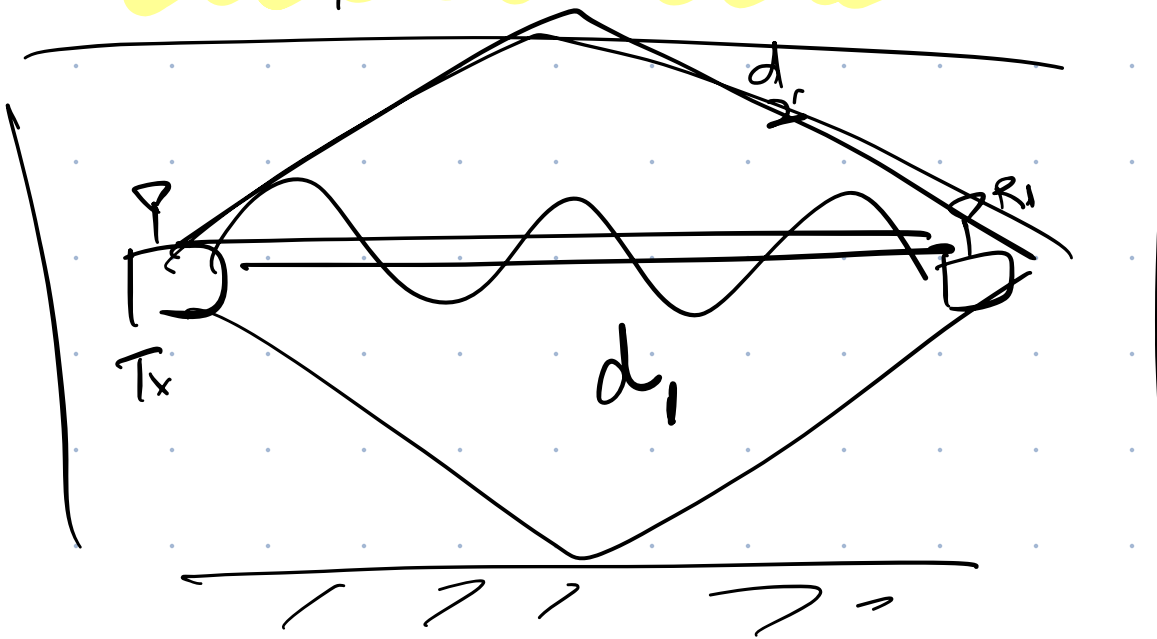
phase



$$\angle h = \frac{2\pi}{\lambda} d \text{ mod } 2\pi$$



Multipath Channel



2 copies of the signal

d_1 , d_2

→ attenuation is nearly the same.

$$y_1 = h(d_1) x_1 + h(d_2) x_1$$

$$= a e^{j \frac{2\pi}{\lambda} d_1} x_1 + a e^{j \frac{2\pi}{\lambda} d_2} x_1$$

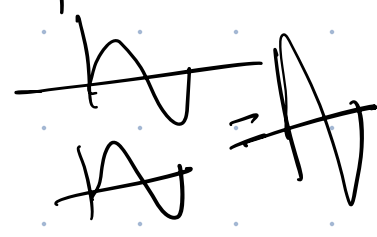
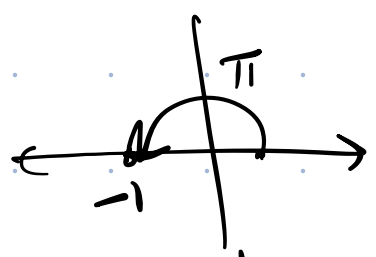
$a e^{j\phi}$
amplitude

$$= a e^{j \frac{2\pi}{\lambda} d_1} x_1 \left(1 + e^{j \frac{2\pi}{\lambda} (d_2 - d_1)} \right)$$

$$1 + e^{j \frac{2\pi}{\lambda} (d_2 - d_1)}$$

$$d_2 = d_1$$

$$= 2a e^{j \frac{2\pi}{\lambda} d_1} \cos \alpha$$



5GHz

$$d_2 - d_1 \approx \frac{\lambda}{2}$$

[3cm]

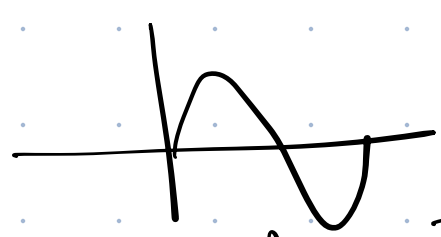
$$1 + e^{j \frac{2\pi}{\lambda} (\frac{\lambda}{2})}$$

$$= 1 + e^{j\pi}$$

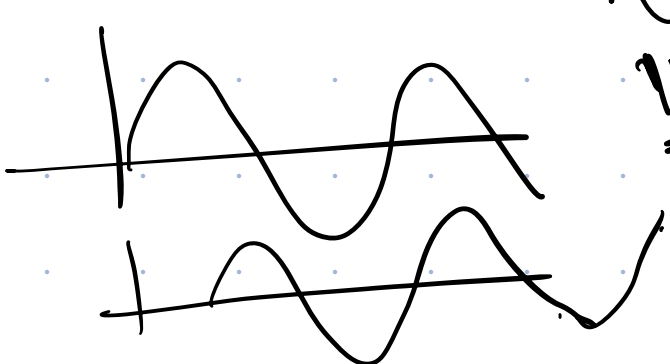
$$= 1 + (-1)$$

$$= 0$$

$$= 0$$



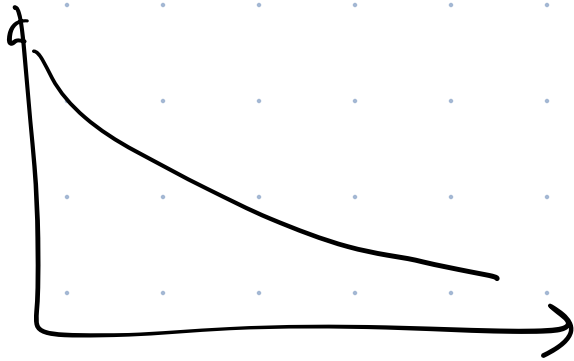
$$= 0$$



$$d_2 - d_1 = \lambda/2$$

$$\lambda_2 = \cancel{\lambda_1}, \lambda/2$$

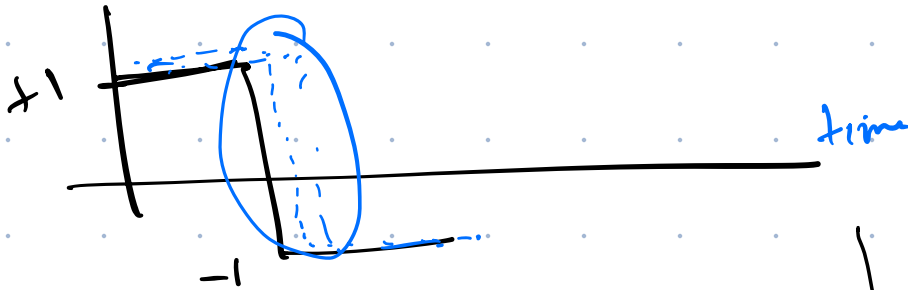
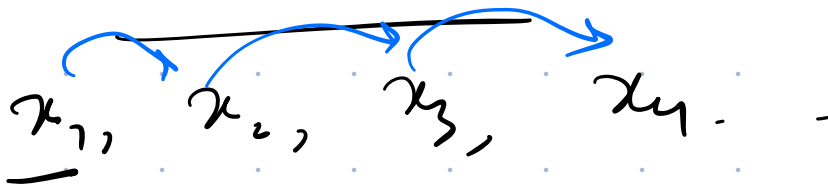
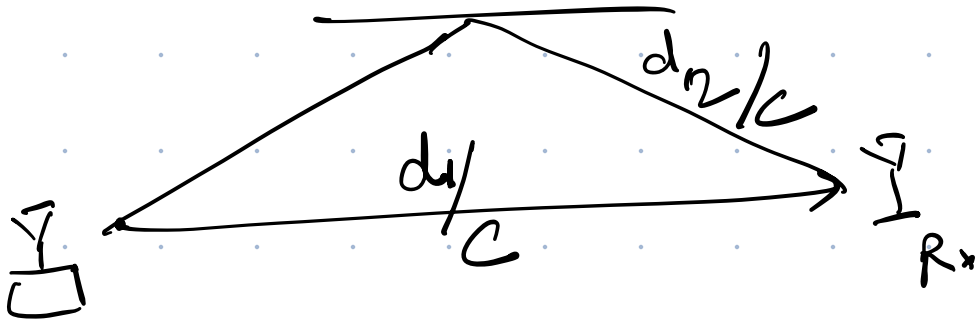
$$d_2 - d_1 = \cancel{\lambda_1} = \cancel{\lambda} \quad \lambda_2$$



Bandwidth \rightarrow Inter-Symbol Interference

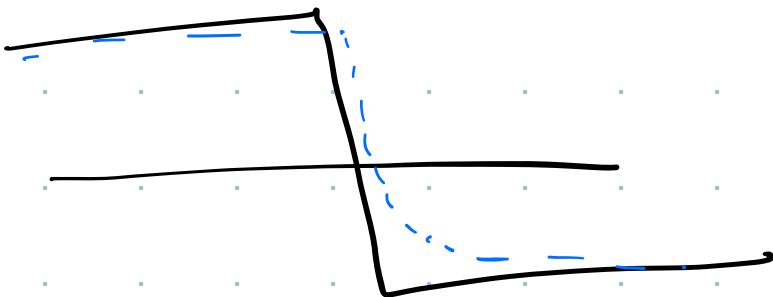
(ISI)

delay



~~low~~ low bandwidth
 $1\text{ kHz} \rightarrow 1\text{ ms}$

$100\text{ MHz} \rightarrow 10^{-8}\text{ s}$
 $\rightarrow 10\text{ ns}$



Narrowband vs. Wideband

OFDM: Motivation